# CALCULATION OF THE CROSS SECTION FOR THE REACTION $\gamma^{3} \mathrm{He} \rightarrow$ pd AT INTERMEDIATE PHOTON ENERGIES 

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#### Abstract

The differential cross section and the asymmetry coefficient for the two-body photodisintegration of ${ }^{3} \mathrm{He}$ by linearly polarized photons are calculated with wave functions for Bonn potential. Dependences of the observables on the components of the ${ }^{3} \mathrm{He}$ wave function with the orbital angular momenta $L, 1^{3} 1$ are studied at photon energies $\mathrm{E}_{\mathrm{g}}$ up to 300 MeV .

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Mechanisms of the reaction $\mathrm{g}^{3} \mathrm{He} ®$ pd and protondeuteron radiative capture at intermediate energies were explored in Refs. [1-9]. In these articles 3 N bound state wave functions (WFs) for realistic nucleon-nucleon potentials were used and plane wave approximation for pd-system was accepted. Role of rescattering effects was studied only in restricted area of photon energies $\mathrm{E}_{\gamma} \leq 139.1 \mathrm{MeV}$ [10-12]. While calculations [1-6,9] were performed with Hannover-Helsinki WF [13] for the Reid soft core (RSC) potential, recent investigations [10-12] were carried out with the rigorous solutions of the 3 N Faddeev equations for modern models of nuclear forces, e.g., Argonne, Nijmegen and CD-Bonn potentials.

Consistency of the interaction currents and the model of nuclear forces was shown to be important $[3,4,6,9$, 11, 12] in calculations of cross sections and polarization observables. Thus, meson exchange currents (MEC) for Argonne potential were used in $[11,12]$ to respect the requirement of gauge independence of the reaction amplitudes.

Along with the relativistic effects originated from meson exchange, manifestation of the spin-orbit electromagnetic interaction of nucleons was studied in [9,14]. It was demonstrated that inclusion of the spin-orbit current (SOC) led to increase of $\Sigma$ values reducing divergence between theory and experiment at $\mathrm{E}_{\gamma}>100 \mathrm{MeV}$.

Role of gauge invariance and Lorentz covariance was studied in $[15,16]$ where a model to account for a part of MEC contributions and the pd-rescattering effects was suggested. By construction $[15,16]$ the reaction amplitudes satisfy the continuity equation. The amplitudes are expressed in terms of $\mathrm{pd}^{3} \mathrm{He}$ vertex function and pd scattering phase shifts.

The aim of the present work is to extend calculations [ $3,4,6,9,14]$ taking advantage of the precise numerical solution of the Faddeev equations for the ${ }^{3} \mathrm{He}$ WF obtained by Bochum-Cracow group [17-19] for Bonn potential and to inquire into dependence of the differential cross section and the asymmetry coefficient on the WF components considering the reaction at intermediate energies $\mathrm{E}_{\mathrm{g}} £ 300 \mathrm{MeV}$.

The amplitudes of the reaction are calculated within approach $[3,4,6,9,14]$ without any multipole expansion for the nuclear current. The contributions of the MEC
are expressed in terms of six-dimensional integrals evaluated numerically.

The Riska model of the $\pi$-meson exchange currents $(\pi \mathrm{EC})$ is used for the two-body part of the nuclear current. The pion-nucleon form factors in MEC are taken in the monopole form with the cut-off parameter $\Lambda_{\pi}=1.2 \mathrm{GeV} / \mathrm{c}$.


Fig. 1. The differential cross section $\sigma=d \sigma / d \Omega{ }_{p}^{c m}$ for ${ }^{3} \mathrm{He}(\gamma, \mathrm{p}) \mathrm{d}$ and the asymmetry coefficient for the reaction with linearly polarized photons at a proton emission angle $\theta_{p}^{c m}=90^{\circ}$. The experimental data $\square,, \square$, and " are taken from [20, 7,8, 1, 2, 5] and [21], respectively

The results obtained with Bochum-Cracow WFs [17-19] for Bonn potential are shown in Figs. 1 and 2 for different sets of the partial wave components in the ${ }^{3} \mathrm{He}$ WF. The number of the partial wave channels taken into account in decomposition of the WF is $\mathrm{N}_{\alpha}$, where $\alpha$ denotes quantum numbers in ( jJ )-coupling (see, e.g., [19]). Two S-waves are retained in the decompositions of the WF for $\mathrm{N}_{\alpha}=2$, D-waves with the orbital angular momenta $\mathrm{Ll}=20,02,22$ are turned on in the case of $\mathrm{N}_{\alpha}$ $=5, \mathrm{P}$-waves for total angular momentum in the twobody subsystem $\mathrm{J}=0,1$ are added in the set $\mathrm{N}_{\alpha}=10$. The
set $\mathrm{N}_{\alpha}=18$ (34) includes the components with $\mathrm{J} £ 2$ (4) and positive parity.

As is seen from Fig. 1, the energy dependence of the cross section $\sigma$, obtained with convection current (CC), spin current (SC) and S-waves in the ${ }^{3} \mathrm{He}$ WF, has deep minimum near $\mathrm{E}_{\gamma}^{\mathrm{lab}}=172 \mathrm{MeV}$. This distinctive feature


Fig. 2. Angular distribution of the differential cross section and the asymmetry coefficient at $E_{\gamma}^{l a b}=$ 208 MeV . Notation for the curves is the same as in Fig. 1. Points. and $\square$ are taken from [7] and [8]. Data. were obtained in [1, 2, 5] at $E_{\gamma}^{\text {lab }}=200 \mathrm{MeV}$
of $\sigma\left[\mathrm{CC} ; \mathrm{SC} ; \mathrm{N}_{a}=2\right]$ is observed in the angular dependence displayed in Fig. 2 as well. Note, that in plane wave approximation $\sigma[\mathrm{CC} ; \mathrm{SC}] \equiv \sigma[\mathrm{CC}]++\sigma[\mathrm{SC}][6,9]$.

MEC smooth both the energy and angular distributions of the cross section $\sigma\left[\mathrm{CC} ; \mathrm{SC} ; \mathrm{N}_{a}=2\right]$ filling these minima. The appreciable difference between the values of $\sigma[C C ; S C]=8.85 \cdot 10^{-4} \mu \mathrm{~b} / \mathrm{sr}$ for $\mathrm{N}_{a}=2$ and $9.88 \cdot 10^{-2} \mu \mathrm{~b} / \mathrm{sr}$ for $\mathrm{N}_{\alpha}=34$ in minimum at $\mathrm{E}_{\gamma}=172 \mathrm{MeV}$ and $\theta_{p}^{c m}=90^{\circ}$ is substantially reduced when $\pi \mathrm{EC}$ are included. Really, we have $\sigma[C C ; \pi E C ; S C]=0.433 \mu \mathrm{~b} / \mathrm{sr}$ and $0.384 \mu \mathrm{~b} / \mathrm{sr}$, for $\mathrm{N}_{\alpha}=2$ and $\mathrm{N}_{\alpha}=34$, respectively. One can arrive at conclusion that contributions of MEC increase the differential cross section at $\theta_{p}^{c m}=90^{\circ}$ mainly due to absorption of photons by neutron-proton pairs moving with relative angular momentum equal to zero.

The beam asymmetry depicted in lower panels of Figs. 1-4 is defined as $\Sigma=\left(\sigma_{00}-\sigma_{\square}\right) /\left(\sigma_{00}+\sigma_{\square}\right)$, where the cross section of the reaction with photons polarized in the reaction plane (perpendicular to the plane) is denoted by $\sigma_{00}\left(\sigma_{0}\right)$.

The asymmetry $\Sigma[\mathrm{CC} ; \mathrm{SC}]$ as a function of photon energy changes qualitatively when D -wave states are added to S-wave ones (cf. curves for $\mathrm{N}_{\alpha}=2$ and $\mathrm{N}_{\alpha}=5$ in

Fig. 1). Sensitivity of $\Sigma$ to the partial waves with $\alpha>2$, unlike to the case of the cross section, survives after inclusion of the $\pi \mathrm{EC}$.

Reducing to some extent the discrepancies between calculated and measured values of the cross sections (Figs. 1 and 2), $\pi \mathrm{EC}$ change the sign of the asymmetry in a vide energy region that is at variance with Kharkov [1,2,5] and Frascati [21] data.


Fig. 3. Relative role of $C C$ and $\pi E C$ in angular distributions of $\sigma_{0 \square}, \sigma_{\square}$ and the asymmetry coefficient at $E_{\gamma}^{l a b}=208 \mathrm{MeV}$


Fig. 4. The same as in Fig. 2. Shown are effects of the spin-orbit electromagnetic interaction with nucleons

As is known $[9,14]$ neither pionic nor seagull MEC interfere with SC or SOC when final state interaction (FSI) is neglected. Coherent contributions of CC and $\pi \mathrm{EC}$ are plotted in Fig. 3. Influence of CC on $\sigma_{\perp}$ is very small and $\sigma$
is entirely determined by $\pi \mathrm{EC}$. Comparison of angular distributions of $\sigma$ calculated with full inclusion of the rescattering effects [11,12] with results obtained in plane wave approximation indicates the great importance of the effects of FSI at energies $\mathrm{E}_{\curlyvee} \sim 70-130 \mathrm{MeV}$. One can infer that FSI compensates increase of the cross section due to MEC. So, it can be expected that the destructive interference of FSI and MEC can affect the asymmetry coefficient changing its behavior.

Following [9, 14], the SOC has been included into present calculations. Inclusion of MEC results (see Fig. 4) in considerable decrease of relative role of the SOC effects. It turns out that influence of SOC can be enhanced if one uses 'soft' pion-nucleon form factors with cut-off parameter, e.g., $\Lambda_{\pi}=4 \mathrm{~m}_{\pi}$ (the corresponding curves are not shown here). However, the Riska model of $\pi \mathrm{EC}$ with $\Lambda_{\pi}=4 \mathrm{~m}_{\pi}$ is hardly consistent with Bonn potential since $\Lambda_{\pi}=1.3 \mathrm{GeV} / \mathrm{c}$ is chosen in the later. It should be noted that according to our calculations variations of the cut-off parameter in the interval $1.2 \leq \Lambda_{\pi} \leq 1.3 \mathrm{GeV}$ very slightly modify the values of the observables within the energy region discussed.

In summary, it is demonstrated that $\pi \mathrm{EC}$ manifest themselves mainly in transitions from the S-states of ${ }^{3} \mathrm{He}\left(\mathrm{N}_{a}=2\right)$ substantially increasing the cross section values. Angular distributions of the cross section at $\theta_{p}^{c m} \square 120^{\circ}$ are insensitive to inclusion of partial wave components of ${ }^{3} \mathrm{He}$ WF with the orbital angular momenta $\mathrm{L}, \mathrm{l}>0\left(\mathrm{~N}_{\mathrm{a}}>2\right)$.

The relative role of the states with $\alpha>2$ is enhanced in the case of the asymmetry coefficient. This observation allows one to hope that reaction $\gamma^{3} \mathrm{He} \rightarrow$ pd with linearly polarized photons provides a strict and sensitive testing ground for exploring structure of 3 N bound state. Surely, consideration of relevant reaction mechanisms, first of all, the rescattering in the final pd-state and three-nucleon photoabsorption is of great interest for interpretation of the data both for the cross section and the asymmetry coefficient.

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