

$$\begin{aligned}
c_{ij} &- & j & ; \\
d_{ij} &- & j & ; \\
h_i^A &- & ; \\
h_{ij} &- & j; \\
h_i^Z &- & ; \\
g_i^{A_1} &- & ; \\
g_{ij} &- & ; \\
j; & & & \\
g_i^{Z_1} &- & ; \\
g_i^{A_2} &- & ; \\
g_i^{Z_2} &- & ; \\
x_i^1 &- & , & ; \\
x_i^2 &- & , & ; \\
; & & & \\
y_{ij} &- & , & j \\
; & & ; & \\
z_{ij} &- & , & j \\
. & & &
\end{aligned}$$

$$F = \sum_{p=1}^2 \left(\sum_{i=1}^m a_i^p x_i^p - \sum_{i=1}^m b_i^p x_i^p \right) - \sum_{i=1}^m \sum_{j=1}^k c_{ij} y_{ij} - \sum_{i=1}^m \sum_{j=1}^l d_{ij} z_{ij} \rightarrow \max .$$

$$\sum_{p=1}^2 x_i^p \leq h_i^A + \sum_{j=1}^k h_{ij} y_{ij} , \quad = 1, 2, \dots, m.$$

$$h_i^A + \sum_{j=1}^k h_{ij} y_{ij} \leq h_i^Z , \quad = 1, 2, \dots, m.$$

$$x_i^1 \leq g_i^{A_1} + \sum_{j=1}^l g_{ij} z_{ij} , \quad = 1, 2, \dots, m.$$

$$g_i^{A_1} + \sum_{j=1}^l g_{ij} z_{ij} \leq g_i^{Z_1} , \quad = 1, 2, \dots, m.$$

$$g_i^{A_2} \leq x_i^2 \leq g_i^{Z_2} , \quad = 1, 2, \dots, m.$$

$$x_i^1 \geq 0, x_i^2 \geq 0, \quad = 1, 2, \dots, m;$$

$$y_{ij} \geq 0, \quad = 1, 2, \dots, m; j = 1, 2, \dots, k;$$

$$z_{ij} \geq 0, \quad = 1, 2, \dots, m; j = 1, 2, \dots, l.$$

$$y_{ij} - , \quad = 1, 2, \dots, m; j = 1, 2, \dots, k;$$

$$z_{ij} - , \quad = 1, 2, \dots, m; j = 1, 2, \dots, l.$$

$$m = 4$$

. 1

(): 1

(A^1)	(B^1)	(A^2)	(B^2)
42	32	19	15
46	34	20	16
82	58	–	–
–	–	22	17

$$k = 2$$

. 2

2

(C)		(H^A)	(H)		(H^Z)
40	35	140	2	1	150
36	32	70	3	2	80
30	28	20	3	3	25
25	24	10	4	3	15

$$l = 3$$

. 3

3

(D)			(G^{A1})	(G)			(G^{Z1})
30	20	15	5	2	3	2	10
25	18	14	4	2	2	1	9
20	15	12	4	1	2	1	8
18	12	0	3	1	1	0	8

. 4

(G^{A2})	(G^{Z2})
100	150
50	70
0	25
8	12

$$F = 10 \cdot x_1^1 + 12 \cdot x_2^1 + 24 \cdot x_3^1 + 4 \cdot x_1^2 + 4 \cdot x_2^2 + 5 \cdot x_4^2 - 40 \cdot y_{11} - 36 \cdot y_{21} - 30 \cdot y_{31} - 25 \cdot y_{41} - 35 \cdot y_{12} - 32 \cdot y_{22} - 28 \cdot y_{32} - 24 \cdot y_{42} - 30 \cdot z_{11} - 25 \cdot z_{21} - 20 \cdot z_{31} - 18 \cdot z_{41} - 20 \cdot z_{12} - 18 \cdot z_{22} - 15 \cdot z_{32} - 12 \cdot z_{42} - 15 \cdot z_{13} - 14 \cdot z_{23} - 12 \cdot z_{33}.$$

$$\begin{aligned} x_1^1 + x_2^1 - 2 \cdot y_{11} - y_{12} & 140; \\ x_1^1 + x_2^1 - 3 \cdot y_{21} - 2 \cdot y_{22} & 70; \\ x_1^1 + x_3^1 - 3 \cdot y_{31} - 3 \cdot y_{32} & 20; \\ x_1^1 + x_4^1 - 4 \cdot y_{41} - 3 \cdot y_{42} & 10; \\ 2 \cdot y_{11} + y_{12} & 10; \\ 3 \cdot y_{21} + 2 \cdot y_{22} & 10; \\ 3 \cdot y_{31} + 3 \cdot y_{32} & 5; \\ 4 \cdot y_{41} + 3 \cdot y_{42} & 5; \\ x_1^1 - 2 \cdot z_{11} - 3 \cdot z_{12} - 2 \cdot z_{13} & 5; \\ x_2^1 - 2 \cdot z_{21} - 2 \cdot z_{22} - z_{23} & 4; \\ x_3^1 - z_{31} - 2 \cdot z_{32} - z_{33} & 4; \\ x_4^1 - z_{41} - z_{42} & 3; \\ 2 \cdot z_{11} + 3 \cdot z_{12} + 2 \cdot z_{13} & 5; \\ 2 \cdot z_{21} + 2 \cdot z_{22} + z_{23} & 5; \\ z_{31} + 2 \cdot z_{32} + z_{33} & 4; \\ z_{41} + z_{42} & 5; \\ x_1^2 & 150; \\ x_2^2 & 70; \\ x_3^2 & 25; \\ x_4^2 & 12; \\ x_1^2 & 100; \\ x_2^2 & 50; \\ x_3^2 & 0; \\ x_4^2 & 8. \end{aligned}$$

$$\begin{aligned} x_i^1 \geq 0, x_i^2 \geq 0, & \quad i = 1, 2, 3, 4; \\ y_{ij} \geq 0, & \quad i = 1, 2, 3, 4; j = 1, 2; \\ z_{ij} \geq 0, & \quad i = 1, 2, 3, 4; j = 1, 2, 3. \end{aligned}$$

$$\begin{aligned} y_{ij} - & \quad i = 1, 2, 3, 4; j = 1, 2; \\ z_{ij} - & \quad i = 1, 2, 3, 4; j = 1, 2, 3. \end{aligned}$$

[1, 175].

Visual Basic
(.5-7).

Microsoft Excel.

$x_i^1 \quad x_i^2, \dots$

(X^1)	(X^2)
5	135
4	66
8	0
0	10

y_{ij}

(Y)	
0	0
0	0
0	0
0	0

z_{ij}

(Z)		
0	0	0
0	0	0
0	2	0
0	0	0

$F_{(0)}^* = 1\ 114$

$z_{32} = 2$

$F_{(0)} = 1\ 048$

6,3%.

1.

20%.

):

(. 9).

1

A^1	B^1	A^2	B^2	C		H^A	H		H^Z	D			G^{A1}			G			G^{Z1}	G^{A2}	G^{Z2}
42	32	19	15	40	35	140	2	1	150	30	20	15	5	2	3	2	10	80	120		
46	34	20	16	36	32	70	3	2	80	25	18	14	4	2	2	1	9	40	56		
82	58	-	-	30	28	20	3	3	25	20	15	12	4	1	2	1	8	0	20		
-	-	22	17	25	24	10	4	3	15	18	12	0	3	1	1	0	8	6,4	9,6		

9

1

X^1	X^2	Y		Z		
10	120	0	0	0	1	1
8	56	0	0	0	2	0

8	0	0	0	0	2	0
0	9,6	0	0	0	0	0

$F_{(1)}^* = 1\ 039$. . .
 $F_{(0)}^* = 1\ 114$. . .
 6,7% . . .

(: $z_{12} = 1; z_{13} = 1; z_{22} = 2; z_{32} = 2$).

$F_{(1)} = 946$. . .
 $x_1^1 \quad x_3^1$

1 3.

2. 30%.

(. 10).

10

2

A^1	B^1	A^2	B^2	C		H^A	H		H^Z	D			G^{A1}	G			G^{Z1}	G^{A2}	G^{Z2}
42	32	19	15	40	35	140	2	1	150	30	20	15	6,5	2	3	2	13,0	100	150
46	34	20	16	36	32	70	3	2	80	25	18	14	5,2	2	2	1	11,7	50	70
82	58	-	-	30	28	20	3	3	25	20	15	12	5,2	1	2	1	10,4	0	25
-	-	22	17	25	24	10	4	3	15	18	12	0	3,9	1	1	0	10,4	8	12

(. 11).

11

2

X^1	X^2	Y		Z		
6,5	133,5	0	0	0	0	0
5,2	64,8	0	0	0	0	0
10,2	0,0	0	0	0	2	1
0,0	10,0	0	0	0	0	0

$F_{(2)}^* = 1\ 173,4$. . . 5,3% . . .

$F_{(0)}^* = 1\ 114$. . . 7,1% . . .

$F_{(2)} = 1\ 095,4$. . . $z_{ij} = 0$.

17 . . . 21,9 . . .

290 372,2 . . . 28,3% . . .

3.

. 12.

12

3

A^1	B^1	A^2	B^2	C		H^A	H		H^Z	D			G^{A1}	G			G^{Z1}	G^{A2}	G^{Z2}
42	32	19	15	40	35	140	2	1	150	30	20	15	5	2	3	2	10	100	150
46	34	20	16	36	32	70	3	2	80	25	18	14	4	2	2	1	9	50	70
82	58	-	-	30	28	20	3	3	25	20	15	12	4	1	2	1	8	0	25
41	30	22	17	25	24	10	4	3	15	18	12	0	3	1	1	0	8	8	12

13).

(.

13

3

X^1	X^2	Y		Z		
-------	-------	---	--	---	--	--

5	135	0	0	0	0	0
4	66	0	0	0	0	0
8	0	0	0	0	2	0
3	11	1	0	0	0	0

$$F_{(3)}^* = 1\,127 \quad \dots \quad 1,2\%$$

$$F_{(0)}^* = 1\,114 \quad \dots$$

$$y_{41} = 1.$$

$$F_{(3)} = 1\,060 \quad \dots$$

6,3%.

4.

10%.

50%. . 14

14

4

A^1	B^1	A^2	B^2	C		H^A	H		H^Z	D			G^{A1}			G		G^{Z1}	G^{A2}	G^{Z2}
42	32	19	15	20	17,5	126	2	1	150	30	20	15	5	2	3	2	10	100	150	
46	34	20	16	18	16	63	3	2	80	25	18	14	4	2	2	1	9	50	70	
82	58	–	–	15	14	18	3	3	25	20	15	12	4	1	2	1	8	0	25	
–	–	22	17	12,5	12	9	4	3	15	18	12	0	3	1	1	0	8	8	12	

(. 15).

15

4

X^1	X^2	Y				Z			
5	121	0	0	0	0	0	0	0	
4	59	0	0	0	0	0	0	0	
8	0	0	0	0	0	2	0	0	
0	12	0	1	0	0	0	0	0	

$$F_{(4)}^* = 1\,028 \quad \dots \quad 7,7\%$$

$$F_{(0)}^* = 1\,114 \quad \dots$$

$$y_{42} = 1.$$

$$(y_{ij} = 0 \quad z_{ij} = 0),$$

$$F_{(4)} = 959 \quad \dots$$

7,2%).

5.

10%.

(. 16).

16

5

A^1	B^1	A^2	B^2	C		H^A	H		H^Z	D			G^{A1}			G		G^{Z1}	G^{A2}	G^{Z2}
42	28,8	19	15	40	35	140	2	1	150	30	20	15	5	2	3	2	10	100	150	
46	30,6	20	16	36	32	70	3	2	80	25	18	14	4	2	2	1	9	50	70	
82	52,2	–	–	30	28	20	3	3	25	20	15	12	4	1	2	1	8	0	25	
–	–	22	17	25	24	10	4	3	15	18	12	0	3	1	1	0	8	8	12	

5

X^1	X^2	Y		Z		
10	130	0	0	0	1	1
8	62	0	0	0	2	0
8	0	0	0	0	2	0
0	10	0	0	0	0	0

1,

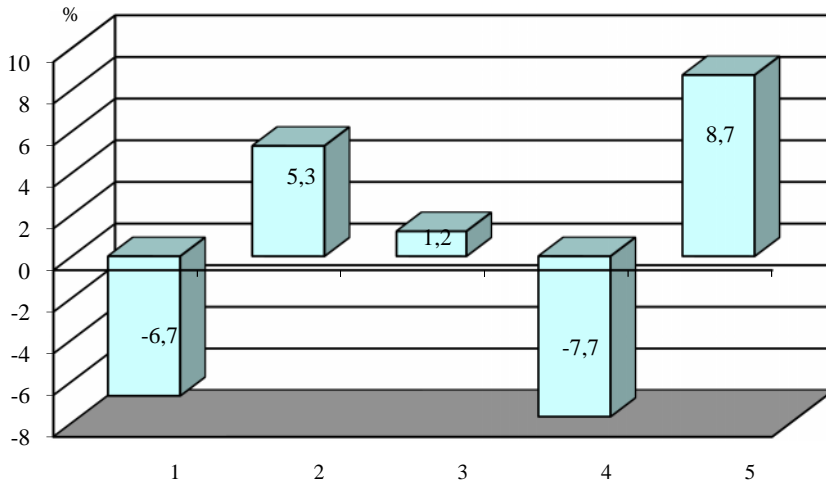
(1,

: $z_{12} = 1$; $z_{13} = 1$; $z_{22} = 2$; $z_{32} = 2$).

$F_{(5)}^* = 1\ 210,6$ 8,7%

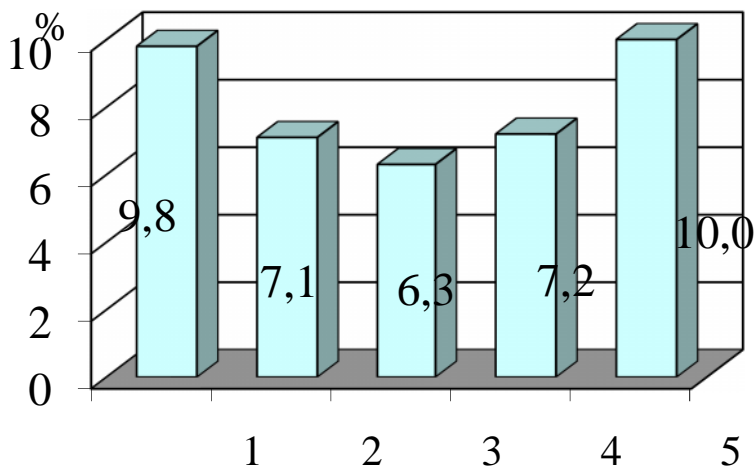
$F_{(0)}^* = 1\ 114$ $F_{(5)} = 1\ 101$ 10,0%.

(. 1).



. 1. /

(. 2).



. 2.

/ , (,).

1. : / - : , 1986. - 192 .
2. : / - : , 2003. - 524 .
3. - / - : , 2005. - 208 .
4. / - : , 2002. - 449 .
5. (: 08.06.04 / ; - . - , 2001. - 24 .):
6. / - : , 2003. - 269 .
7. : / - : , 2003. - 282 .

07.10.2010 .