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# New Automaton-Game Theory Method for Modeling of Reliability and Flexibility Valuation for CAD-CAM Systems

The method of reliability and flexibility valuation for computer aided design and flexible manufacture interpreted as an indivisible purposeful system, which is based on purposeful automaton theory, automaton-game simulation of design and cluster analyses, developed by the authors, is also investigated herein. The necessity to develop adaptable self-training systems for the study of these units is grounded.

## Introduction

Computer aided design (CAD) and flexible manufacturing systems (FMS) for computer aided manufactory (CAM) are now considered to be of the highest engineering level. Although the major part of the research in this field is divided into two separate directions, concerning CAD and CAM. This fact contradicts the system theory approach.

In this paper some features of CAD-CAM, which determine their efficiency and expedience, are discussed. The basic principles for this are: purposefulness, evolution ability, system analysis, complexity and man-computer integration [1], [2], [3].

**Task definition.** Let general aim  $F_s$  to create system  $S$ , which has a number of characteristics  $H_s$  as well as resources  $R_s$  and time-limit  $T_s$ , be formulated and besides

$$F_s = (f_1, \dots, f_i, \dots, f_n),$$

where  $f_i$  is local aims (criteria).

The aim  $F_s$  is achieved. If  $T_s^* \leq T_s$ ,  $R_s^* \leq R_s$ ,

$$f_i^* = \text{opt } f_i \text{ I } (H_s, R_s, T_s) \text{ for all } i = 1, \dots, n, \quad (1)$$

where  $T_s^*$ ,  $R_s^*$ ,  $f_i^*$  are actual values for design-time, resources and local aims. Now we want to select the factors, which first of all influence the task (1), expected to be solved by CAD-FMS unit; further this unit is referred to as CAD-CAM.

## Models and Methods

Automaton-game model. Let's observe the discrete process of designing and creating system  $S$ . Design problem is described as purposeful finite discrete indeterminate automaton functioning [1], [4]:

$$A_1 = \langle X_1, Y_1, Z_1, \xi_1, \psi_1, F_1 \rangle, \quad (2)$$

where  $X_1$ ,  $Y_1$ ,  $Z_1$  are inputs, outputs and state factors,

$\xi_1 = X_1 \times Z_1 \times F_1 \Rightarrow Z_1$  is transaction function,  $\psi_1 = X_1 \times Z_1 \times F_1 \Rightarrow Y_1$  – outputs function,  $F_1$  is the aim of system S design,  $F_1$  belong to  $F_s$ .

The manufacturing problem can be given in the same way

$$A_2 = \langle Y_1, Y_2, Z_2, \xi_2, \psi_2, F_2 \rangle, \tag{3}$$

where  $\xi_2 = Y_1 \times Z_2 \times F_2 \Rightarrow Z_2$ ,  $\psi_2 = Y_1 \times Z_2 \times F_2 \Rightarrow Y_2$ .

On the whole the constructing of S is realized by the automaton  $A_0$  :

$$A_0 = A_1 \cup A_2,$$

or

$$A_0 = \langle X_1, Y_2, Z, \xi_0, \psi_0, F_s \rangle, \tag{4}$$

$$Z = Z_1 \cup Z_2, \quad \xi_0 = X_1 \times Z \times F_s \Rightarrow Z, \quad \psi_0 = X_1 \times Z \times F_s \Rightarrow Y_2.$$

The  $A_0$ -automaton processes data, energy and materials, therefore it consists of three local automata  $A_i$ ,  $A_l$ ,  $A_m$  described in (1), (2):

$$A_0 = A_i \cup A_l \cup A_m. \tag{5}$$

The models (2)-(5) formulate the whole engineering problem in terms of purposeful technological designer activity. The structure of automaton (2) examples the set of sub automata  $A_{1d}$ ,  $A_{1r}$ ,  $A_{1c}$ , which represent supervisor, computer and controller, fig.1.

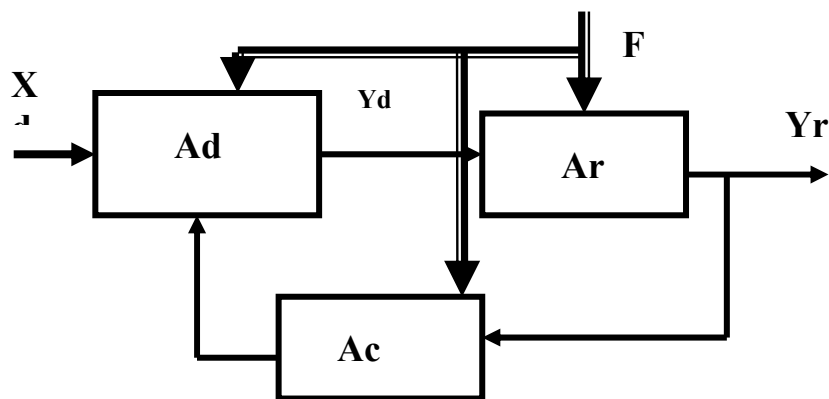


Figure1. A common model of automata ergamat, where  $A_d$  is subautomata supervisor,  $A_r$ - subautomata is computer,  $A_c$  is subautomata-controller,  $F$  is aim of system

Thus, the automata (2), (3) possess all general features of actual control systems; that's why model (2) can simulate the CAD and (3) can simulate the FMS-CAM-systems. Hence, figure (4) is the model of CAD-CAM. The functions  $\xi_0$ ,  $\psi_0$  are the most complex members in the automaton  $A_0$ . For their playing models of vector-games (V-games) are used [2]. In general a V-game is defined as follows

$$G = \langle \{I_k\}, \{N_k\}, \{F_k\}, \{R_k\}, \pi \rangle, \tag{6}$$

where  $I_k$  is any gambler from the set  $\{I_k\}$  which has it's own vector-strategy  $N_k$ , aim  $F_k$  and resource  $R_k$ ;  $\pi$  is game rules. The local aims  $F_k$  in a complex hierarchical man-computer CAD CAM-system are not collinear, but subordinate to general purpose  $F_s$ . Therefore approaching the aim  $F_s$  under conditions (1) (or evolution of the automata (2), (3), (4), (5) ) can be interpreted as running of the finite V-games set (6), defined on some net

structure of Ao-automaton [1], [2]. After that follows  $\xi_0 \approx G\xi$ ,  $\psi_0 \approx G\psi$ , where  $G\xi$ ,  $G\psi$  are V-games, which causes changing the state Z and outputs Y2 for Ao then figure (4) shows

$$A_0 = \langle X1, Y2, Z, G\xi, G\psi, Fs \rangle. \quad (7)$$

The model (7) is called automaton-game model (AG-model) for CAD-CAM. The aims  $Fx$ , which appear in  $A_0$ , are vectors too, that is  $Fk = (fk_1, \dots, fk_n)$ . Some reasons of conflicts among the members of  $A_0$  have been investigated earlier [2]. For a couple of gamblers  $I_k, II$  I  $F_k, F_l$  the antagonism can be introduced

$$akl(G) = (n - n_0)/n, \quad 0 \leq akl \leq 1,$$

where  $n_0$  is the set amount for those components  $f_{ki}$  belong to  $F_k$  and  $f_{li}$  belong to  $F_l$ , whose interests are collinear,  $n_0 \leq n$ . Obviously, any game is fully antagonistic, if  $n_0 = 0$  or if  $n_0 = n$ , then it is completely non-conflict. That's why  $akl$  can indicate the reliability and flexibility of  $A_1, A_2, A_0$ , and the control strategy for CAD-CAM is how to obtain  $akl \sim$  minimum at each design step and time discrete  $t_i$  belong to  $T_s$ .

**Reliability characteristics definition.** Let the system S be a  $B_s$  composition of members  $b_j$ ,

$$B_s = \{b_j\}, j = 1, \dots, m.$$

Then we divide  $B_s$  into three clusters using the following conditions:  $B_\alpha$  is  $\alpha$ -cluster, if any single failure of member by  $\alpha$  belong to  $B_\alpha$ ,  $B_\alpha$  belong to  $B_s$ , causes the S-failure as a whole.  $B_\beta$  is  $\beta$ -cluster, if any single by  $\beta$ -failure inside the time interval  $[0, t_j\beta]$ ,  $b_j\beta$  belong to  $B_\beta$ ,  $B_\beta = B_s \setminus (B_\alpha \text{ belong to } B_s)$  only decreases the S-efficiency.  $B_\gamma$  is  $\gamma$ -cluster, if no single by  $\gamma$ -failure within  $[0, t_\gamma]$  influences the S-efficiency at all, but all the by  $\gamma$ -failure inside  $[0, t_\gamma]$  or even single one within  $[t_\gamma, t_s]$  decreases S-efficiency. The components by  $\alpha$  belong to  $B_\alpha$  cover the basic structure of S-system. To design some objects from  $B_\alpha, B_\beta, B_\gamma$  there are correspondent clusters  $\alpha_1, \beta_1, \gamma_1$  of subautomata

$$A1\alpha, A1\beta, A1\gamma \text{ for } A1 \text{ and the same are } \alpha_2, \beta_2, \gamma_2 \text{ of } A2\alpha, A2\beta, A2\gamma \text{ for } A2.$$

These clusters realize the design decisions obtained on  $A1\alpha, A1\beta, A1\gamma$ . Let  $T1$  be time interval for S-design,  $T2$  be the interval of design realization on  $A2$ ,  $T2 = T_s - T1$ .

If a single task from  $\alpha_1$ -cluster is unsolved within  $T1$ , then the whole project is considered be not realized. If the same takes place for  $\beta_1$ -cluster, the project is not optimal. Now the project is not realized if no tasks at all from  $\beta_1$ -cluster are solved inside  $T1$ . What's else, we specify the whole project as not-realized, if at least one single task from  $\gamma_1$ -cluster remained unsolved in  $T_s$ . The system S is considered be not-operational if a single decision at least from  $\alpha$ -cluster is not realized through the subautomata  $\alpha_2$  within  $T2$ . The S is not considered optimal if any one decision from  $\beta_1$  has been unaccomplished by the  $\beta_2$ -subautomata in  $T2$ , and S is un operational if all the decisions from  $\beta_1$  are not implemented in  $T2$ . At last, the S is not optimal if all the  $\gamma_1$ -decisions are not realized in  $T2$  or even one of them during the test maintenance within the time discrete  $\Delta t$  belong to  $t_s$ .

The probability  $P\{Fs\}$  of the aim  $F_s$  achievement under conditions (1) depends on the  $A_1, A_2$ -reliability:

$$P\{Fs\} = P(A_1) \cdot P(A_2), \quad (8)$$

where  $P(A_1)$  is non-failure probability for  $A_1$  in  $[0, T1]$ ,  $P(A_2)$  for  $A_2$  in  $[T1, T_s]$ .

According to the concepts of reliability theory we take the consequent way of subautomata connection and the parallel one for the clusters. Then the probabilities of subautomata norm 1 functioning indicate

$$P(\alpha_1) = \prod P(A1\alpha_1), P(\beta_1) \dots \prod P(A2\gamma_6)$$

and now

$$P(A1) = 1 - ((1 - P(\alpha_1)) (1 - P(\beta_1)) (1 - P(\gamma_1))) \quad (9)$$

$$P(A2) = 1 - ((1 - P(\alpha_2)) (1 - P(\beta_2)) (1 - P(\gamma_2))). \quad (10)$$

The A1 mainly transforms the input data X1 into the output Y1. Therefore it's more relevant to Ai' in (5), and now

$$P(A1) = P(Ai).$$

The A2 takes data Y1, the aims F2, Fs and then transforms energy and materials, approaching to S. That's why the A2 is to be described as A1 U Am and  $P(A2) \sim P(A1 \cup Am)$ . From this point of view we shall select factors which have the strongest influence

on  $P(Ai)$  and  $P(A1 \cup Am)$ .

Considering (6), (7) the CAD-CAM functioning can be approximated by the purposeful general exercising of the V-games set, where the P(Fs)-factor somehow depends on the values of  $a_{kl}$  for any couple of interconnected subautomata in A1, A2, on  $a_{12}$  for the couple (A1, A2) and on  $a_{01}$ ,  $a_{02}$  while automata A1, A2 performs V-games with nature-partner (external actions). To solve such games the efficient principle of pattern strategy has been developed. Obviously, antagonism degree of  $a_{kl}$  considerably influences the task solving probability for the subautomata of all the clusters. Thus all the members

$$P(\alpha_1), \dots, P(\gamma_2),$$

are functions of all in their own clusters. The general strategy of Ao-functioning demands completely to eliminate antagonism each step of making decisions. Now if for some couples of subautomata in  $\alpha_1$  or in  $\alpha_2$  cluster is valid

$$a_{kl}\alpha_1 = 1 \text{ or } a_{kl}\alpha_2 = 1 \text{ then } P(A1) = 0 \text{ or } P(A2) = 0$$

what in any case gives  $P(Fs) \neq 0$ . The results in clusters  $\beta_1, \beta_2, \gamma_1, \gamma_2$  are defined in the same way, but herein  $P(Fs) \neq 0$  except the above mentioned case. The problem of antagonism degree elimination in CAD-CAM is under investigated and its research is now very important; this causes new problem of artificial intellect in CAD-CAM.

CAD-CAM readiness. Let's define the factor maintenance-readiness of A1 as

$$K(A1) = (T1 - \sum c t_c) / T1, \quad c = 1, \dots, 6,$$

where  $t_1$  is the time interval necessary for conflicts to be eliminated, which may appear as a consequence of incorrect tasks, indefinite aims or function distribution,  $t_2$  is period within the automaton is waiting for instructions,  $t_3$  is delay time determined by computers and peripheries,  $t_4$  is pauses because of hard- and software defects,  $t_5$  is time spent to locate and prepare the data,  $t_6$  is time for project coordination. For A2 is valid

$$K(A2) = (T2 - \sum t'_c) / T2, \quad c = 1, \dots, 6.$$

$t_3$  is time lost because of hardware;  $t_4$  is time lost, because of the defects appeared in the software of computer controlled machinery and robots, involved in manufacturing

system S;  $t_5$  is time extent necessary for decision correction and mistakes elimination;  $t_6$  – preparation time for the task YI received from A1.

Then

$$K(A_o) = (T_s - \sum t_c - \sum t'_c) / T_s .$$

So the main factors that determine CAD-CAM readiness are: management, efficiency, data- and software quality, machinery reliability.

**CAD-CAM flexibility.** We want to study the flexibility concept in two aspects: in local and general. We define the local flexibility we define as automaton  $A_o$  feature to provide an optimal output  $Y_2$  in  $[O, T_s]$  inspire of  $X_1$  and (or)  $F_s$  changes, while the  $A_o$ -structure is constant. This is functional  $A_o$ -flexibility. We understand the general flexibility as automaton ability quickly tune on the new aim  $F$ 's in  $\Delta \tau$ -time and (or-) on the new input  $X_1$  to get corresponding output  $Y_2$  inside the subject oriented sphere of aims  $\Delta F_s$ . This is structure functional flexibility of  $A_o$ .

To provide the local  $A_o$ -flexibility it is necessary to, develop and use the discrete adaptive self-training system methods known before. Apparently, the general flexibility expects the local one. To study general flexibility we observe CAD-CAM as a queuing system. Here the successive connected  $A_1$  and  $A_2$  are servants. The inputs for  $A_1$  are  $X_1$ ,  $F_s$ . The service manner is determined by the aim  $F_1$  C  $F_s$  and restricted by  $T_1$ ,  $H_s$ ,  $R_1$  belong to  $R_s$ . The inputs for  $A_2$  are  $Y_1$ ,  $F$ ,  $S$ ; the service is also specified by  $F_2$  C  $F_s$  and restricted by  $T_2$ ,  $H_s$ ,  $R_2$  C  $R_s$ . The  $F_s$  has major priority among the inputs of  $A_1$ ,  $A_2$ . Both inputs are non-stationary. The system  $A_1$  starts service actions according  $F$ 's after result  $Y_1$  has been obtained, and  $A_2$  starts after  $Y_2$ . Considering the complexity of automata  $A_1$ ,  $A_2$  structure (whose automata are service subsystems), and man-computer relations of those automata as well, we note following theses (which are not detail discussed in this paper).

1. The functioning of  $A_1$ -input subautomata, which percept  $X_1$  (from surroundings, can be specified as Markov's process in  $[0, \tau]$ .

2. In  $[\tau, \tau_s]$ -interval this process transforms itself into non-Markov's because of:

a) iterate character of  $A_1$ ,  $A_2$  and loops in their connections;

b) multicriterial of project decisions and their starting-point compromise indicate the influence on the whole process of project realizing until the end-point  $Y_2$  |  $F_s$  because of incorrect task and (or) aim formulation.

The automata  $A_1$ ,  $A_2$ ,  $A_o$  reliability can be estimated in two meanings as follows.

1. Let  $t'_s$  be the time interval within the aim  $F_s$  of creating and maintenance new system  $S'$  is constant, e.g.  $S'$  is in a constant demand;  $T_s$  is the interval necessary to create  $S'$  using  $A_o$ ;  $t''$  is the interval for tuning  $A_o$  on the new aim  $F$ 's. Then the flexibility factor is

$$L(A_o) = (t'_s - T_s - t''_s) / t'_s.$$

If  $T_s \geq t'_s$ ,  $t''_s \geq t'_s$  and  $L(A_o)$  is negative, then  $A_o$  can't manufacture computable production. The  $A_o$  is worth if  $0 < L(A_o) < 1$  Factors  $L(A_1)$ ,  $L(A_2)$  are defined the same way. These factors determine the functional flexibility of  $A_o$ .

2. The structure of automaton  $A_o$  can be covered by oriented sectioned net

$$N(A_o) = (V_1, \dots, V_n, \Theta),$$

Where  $V_1, \dots, V_n$  are sections of the net-knots representing the subautomata  $A_o$  from clusters  $\alpha_1, \alpha_2$ ,  $\Theta$  - the set of oriented connections [2], [4];

$n$  is the number of knot sections. The entrance-section  $V_1$  from  $A_1$  takes the input data  $X_1$  |  $F_s$  the aims of subautomata in  $V_1, \dots, V_n$  are determined by  $F_s$ -decomposition; the exit- section  $V_n$  outputs  $Y_2$  |  $F_s$  according to (1).

Thus  $N(A_0)$  is the structure-functional model of CAD-CAM studied as a queuing system. The  $N(A_0)$  can be used for realizing some nets of structures  $W$ : anyone of them is able to provide some output  $Y_{2i}$  while floating  $X_1$  in  $\Delta X_1$ -interval and (or-)  $F_s$  in  $\Delta F_s$  but considering (1). The structure transformation from  $W_i (N(A_0))$  into  $W_k (N(A_0))$  is supposed to occur in jump-manner when the aim  $F_s$ -change quantum is greater than  $\Delta^*F_s$  and (or) input  $X_1$ -change is greater than  $\Delta^*X_1$ . From this point of view the structure flexibility of  $A_0$  can be indicated by the set power of  $W$  -  $L^*(A_0) = 1$ , then  $A_0$  shows only the local flexibility.

## Conclusion

Methodological basis of CADM simulation as automata target aimed systems and methods of determining their reliability, readiness and flexibility are proposed. It is how that investigation of CADM target aimed queuing systems is worthy of note. The proposed method of  $\alpha$ ,  $\beta$ ,  $\gamma$ -clustering for CADM tasks and functions allows to classify demands upon CADM reliability, readiness and flexibility in particular by paying main attention for creating optimum readjustable basic composition.

In our opinion problems of CADM flexibility are actual, but they are more fully reflected in terms of CADM adaptation and self-organizing as power controlling systems. Received results are perspective for developing and use CADM in theory. Limited volume of this paper does not allow us to consider problems of CADM shaping as a queuing system with non-Markov's process of functioning. These problems demand special investigations as they are raised for the first time.

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### **Новий автоматно-ігровий метод моделювання надійності і гнучкості автоматизованих систем проектування і виробництва**

Розглядається новий метод оцінки надійності і гнучкості системи автоматизованого проектування і виробництва як єдиної цілеспрямованої системи на основі синтезованих автоматно-ігрових моделей, розроблених авторами, кластерного аналізу і векторних ігор.

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### **Новый автоматно-игровой метод моделирования надежности и гибкости автоматизированных систем проектирования и производства**

Рассматривается новый метод оценки надежности и гибкости системы автоматизированного проектирования и производства как единой целеустремленной системы на основе синтезированных автоматно-игровых моделей, разработанных авторами, кластерного анализа и векторных игр.

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